सांख्यकी (परारनातक) कार्यक्रम अधिन्यास सत्र 2019–20

Course Code:	Course Title:	Maximum Marks : 30
PGSTAT-01(N)/MASTAT-01(N)	Probability and Distribution	
PGSTAT-02(O)/MASTAT-02(O)		

Section- A

Long Answer Questions

Note: Attempt all questions. Each question should be answered in 800 to 1000 Words.

Maximum Marks: 18

- 1. State and prove central limit theorem.
- 2. Write down the axiomatic definition of probability. Let A, B and C be three events.
- 3. Define characteristic function of random variable. State some of its important properties.

Section - B

Short Answer Questions

Maximum Marks: 12

Note: Write any four questions. Answer should be given in 200 to 300 Words.

- 1. State and prove Jensen inequality.
- 2. Discuss about the random variable and its type.
- 3. Let $\{X_n\}$ be a strictly decreasing sequence of random variables which assume positive values only and suppose that $X_n \xrightarrow{a.s.} 0$
- 4. State and prove Jenson's inequality.

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Course Code:	Course Title:	Maximum Marks : 30
PGSTAT-02(N)/MASTAT-02(N)	Statistical Inference	
PGSTAT-03(O)/MASTAT-03(O)		

Section- A

Long Answer Questions

Note: Attempt all questions. Each question should be answered in 800 to 1000 Words.

Maximum Marks: 18

- 1. State and prove Rao- Blackwell theorem.
- 2. On the basis of random sample of size n from the Poisson distribution with parameter θ , obtain UMVUE of e⁻⁵⁰.
- 3. On the basis of a random sample of size n from the family of normal distributions {N $[\theta,\theta], 0 < \theta < \infty$ }, obtain a minimal sufficient statistic.

Section - B

Short Answer Questions

Note: Answer all questions. Answer should be given in 200 to 300 Words.

- 1. Write short notes on (a) MP tests (b) UMP tests.
- 2. Let $X_1, X_2 X_n$ be a random sample from U $[0, \theta], \theta \in (0, \infty)$. Let $X_{(n)} = Max (X_1, X_2 X_n)$ Show that $X_{(n)}$ is not BAN for θ .
- 3. On the basis of a random sample of size n from the Poisson distribution $P(\theta)$, obtain Cramer Rao lower bound for the variance of unbiased estimator of θ^2 .
- 4. Define the all conditions of a good estimator.

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Course Code:	Course Title:	Maximum Marks : 30
PGSTAT-03(N)/MASTAT-03 (N)	Linear Models and Design of	
PGSTAT-04(O)/MASTAT-04(O)	Experiments	

Section- A

Long Answer Questions

Note: Attempt all questions. Each question should be answered in 800 to 1000 Words.

Maximum Marks: 18

- 1. State and prove Gauss-Markov theorem.
- 2. Discuss about the analysis of covariance and define ANCOVA table.
- 3. Discuss about the Principles of design of experiment.

Section - B

Short Answer Questions

Note: Answer all questions. Answer should be given in 200 to 300 Words.

- 1. Write a brief note on BLUE
- 2. Write a note on contrast and orthogonal contrast.
- 3. Write a note on resolvable design and affine resolvable design.
- 4. Write a note on Parameters of BIBD. Also prove that vr = bk

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Course Code:	Course Title:	Maximum Marks : 30
PGSTAT-04(N)/MASTAT-04(N)	Survey Sampling	
PGSTAT-05(O)/MASTAT-05(O)		

Section- A Long Answer Questions

Note: Attempt all questions. Each question should be answered in 800 to 1000 Words.

Maximum Marks: 18

- 1. Prove that $V(\bar{y}_{sy}) \le V(\bar{y}_{st}) \le V(\bar{y}_{srs})$
- 2. Discuss about the Midzuno and Narian system of sampling.
- 3. Calculate mean and variance of ratio and regression sampling.

Section - B

Short Answer Questions

Note: Answer all questions. Answer should be given in 200 to 300 Words.

- 1. Define Parameter and Statistic.
- 2. Discuss about the advantages and limitations of simple random sampling.
- 3. Write a note on Non Sampling and Sampling error.
- 4. Calculate mean and variance of the SRSWOR.

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Course Code:	Course Title:	Maximum Marks : 30
PGSTAT-05(N)/MASTAT-05(N)	Stochastic Process	
PGSTAT-08(O)/MASTAT-08(O)		

Section- A Long Answer Questions

Note: Attempt all questions. Each question should be answered in 800 to 1000 Words.

Maximum Marks: 18

- 1. For a two state Markov chain, under suitable assumptions, derive the expression for the probability that the process occupies state 1 at time n given that the initial probability vector is $(P_0 P_1)$.
- 2. State and prove the Chapman Kolmogorov equation for a Markov Chain. Giving some counter example, show that the equations are satisfied by non-Markovian processes also.
- 3. Stating the underlying assumptions, give the derivation of a Poisson process.

Section - B

Short Answer Questions

Note: Answer all questions. Answer should be given in 200 to 300 Words.

- 1. Define (i) An Ergodic Markov Chain, (ii) Stationary Markov Chain.
- 2. Find the probability distribution of inter-arrival time for a Poisson process.
- 3. Let C_1 and C_2 be two communicative classes of a Markov chain and "S" be a state, which belongs to C_1 but not C_2 . Prove that C_1 and C_2 are disjoint.
- 4. State (Do not give the proof) fundamental theorem of probability of extinction in Branching Process.

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Course Code:	Course Title:	Maximum Marks : 30
PGSTAT-07(N)/MASTAT-07(N)	Mathematical Analysis	
PGSTAT-01(N)/MASTAT-01(O)		

Section- A

Long Answer Questions

Note: Attempt all questions. Each question should be answered in 800 to 1000 Words.

Maximum Marks: 18

- 1. State & Prove Riemann Stieltjes integrals.
- 2. State & Prove Baire's theorem.
- 3. Define compact spaces & compact sets.

Section - B

Short Answer Questions

Note: Answer all questions. Answer should be given in 200 to 300 Words.

- 1. Write short notes on (a) MP tests (b) UMP tests
- 2. Discuss about the CRK bound.
- 3. Discuss in short (a) BAN estimator (b) CAN estimator
- 4. Discuss about the Bhattacharya bound.

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Course Code:	Course Title:	Maximum Marks : 30
PGSTAT-08(N)/MASTAT-08(N)	Measure Theory	

Section- A

Long Answer Questions

Note: Attempt all questions. Each question should be answered in 800 to 1000 Words.

Maximum Marks: 18

- 1. State and prove Heine-Borel theorem.
- 2. State and prove Fubini's theorem.
- 3. State and prove Radon- Nikodym theorem.

Section - B

Short Answer Questions

Note: Answer all questions. Answer should be given in 200 to 300 Words.

- 1. Define about the Hahn & Jordan decomposition.
- 2. Discuss about the Leibnitz rule.
- 3. Define Borel measurable function and it utility in statistics.
- 4. State and prove Fatou's lemma.

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Course Code:	Course Title:	Maximum Marks : 30
PGSTAT-09(N)/MASTAT-09 (N)	Survival Analysis	

Section- A Long Answer Questions

Note: Attempt all questions. Each question should be answered in 800 to 1000 Words.

Maximum Marks: 18

- 1. Calculate the moment generating function of exponential distribution.
- 2. Write a short note on Desh Pande test.
- 3. Discuss about the life tables. Also construct the life table.

Section - B

Short Answer Questions

Note: Answer all questions. Answer should be given in 200 to 300 Words.

- 1. Write short notes on Mentel Haenzel test & Log rank test.
- 2. Describe Weibull distribution with its first four moments.
- 3. What is Ageing Classes. Write its properties.
- 4. Define survival function. Establish its relationship with hazard function.

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Course Code:	Course Title:	Maximum Marks : 30
PGSTAT-10(N)/MASTAT-10(N)	Reliability Theory	

Section- A

Long Answer Questions

Note: Attempt all questions. Each question should be answered in 800 to 1000 Words.

Maximum Marks: 18

- 1. Write a note on Hollander Proschan and DeshPande test for exponential.
- 2. State and prove Loss of memory property of exponential distribution.
- 3. Estimate the moment generating function distribution. Whether its mean exits.

Section - B

Short Answer Questions

Note: Answer all questions. Answer should be given in 200 to 300 Words.

- 1. Define reliability. Also, differentiate it from quality, clearly.
- 2. What do mean by a coherent system.
- 3. Discuss utility of cut and path sets.
- 4. Describe Reliability function and Hazard rate.

सांख्यकी (परास्नातक) कार्यक्रम अधिन्यास सत्र 2019–20

Course Code:	Course Title :	Maximum Marks : 30
PGSTAT-11(N)/ MASTAT -11(N)	Operation Research	

Section - A Long Answer Questions

Note: Attempt any three questions. Each question should be answered in 800 to 1000 Words. Maximum Marks: 18

- 1. Discuss about the Linear Programming Also Define the different steps for Graphical solution to LPP.
- 2. Write a detailed not on classification of models used in operations research.
- 3. Solve the following LPP :

Section - B

Short Answer Questions

Maximum Marks: 12

Note: Attempt any four questions. Answer should be given in 200 to 300 Words.

- 1. Discuss in brief about the Hungarian method.
- 2. Describe the graphical method for $2 \times n$ or $m \times 2$ games.
- 3. Soles the following LPP graphically (give all steps). Max. Z = 3 x + 2y, subject to $x-y \le 1$, $x+y \ge 3$ and $x, y \ge 0$.
- 4. Write a brief note a various types of variables used in LPP.

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Course Code:	Course Title:	Maximum Marks : 30
PGSTAT-13(N)/MASTAT-13(N)	Decision Theory	
PGSTAT-09(0)/MASTAT-09(0)		

Section- A

Long Answer Questions

Note: Attempt all questions. Each question should be answered in 800 to 1000 Words.

Maximum Marks: 18

- 1. Discuss about the Optimal Decision Rules.
- 2. State and Prove complete class Theorem.
- 3. State is the basic difference between Bayes and Minimax Principles.

Section - B

Short Answer Questions

Note: Answer all questions. Answer should be given in 200 to 300 Words.

Maximum Marks: 12

- 1. Discuss about the Invariance and ordering.
- 2. What is the equalizer rule. Discuss about it.
- 3. Write a note on Extended Bayes Rule.
- 4. Write short notes on (a) Admissibility (b) Completeness

उत्तर प्रदेश राजर्षि टण्डन मुक्त विश्वविद्यालय,प्रयागराज

सांख्यकी (परास्नातक) कार्यक्रम अधिन्यास सत्र 2019–20

Course Code:	Course Title:	Maximum Marks : 30
PGSTAT-14(N)/MASTAT-14(N)	Multivariate Analysis	
PGSTAT-10(0)/MASTAT-10(0)		

Section- A

Long Answer Questions

Note: Attempt all questions. Each question should be answered in 800 to 1000 Words.

Maximum Marks: 18

- 1. Discuss about the Wishart distribution. Also find its additive Property.
- 2. Discuss about the Maholanobis D^2 with its various applications.
- 3. Discuss about multiple and partial correlation coefficient.

Section - B

Short Answer Questions

Note: Answer all questions. Answer should be given in 200 to 300 Words.

- 1. Find the characteristic function of MMD.
- 2. Write short notes on Discriminate Analysis.
- 3. Obtain MLE of mean vector for multivariate normal population.
- 4. Maximum likelihood estimates of mean vector.

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Course Code:	Course Title:	Maximum Marks : 30
PGSTAT-15(N)/MASTAT-15(N)	Nonparametric	
PGSTAT-11(O)/MASTAT-11(O)		

Section- A Long Answer Questions

Note: Attempt all questions. Each question should be answered in 800 to 1000 Words.

Maximum Marks: 18

- 1. Describe two Sample Kolmogorov Smirnov test.
- 2. What do you understand by order statistics? Discuss their role in non-parametric theory. Obtain the joint distribution of maximum and minimum order statistics.
- 3. What do you mean by two sample location test? Discuss sign test for two sample problem.

Section - B

Short Answer Questions

Note: Answer all questions. Answer should be given in 200 to 300 Words.

- 1. Discuss in short about the Median test and Wilcoxan test.
- 2. Write short notes on (a) Run test (b) Sign test.
- 3. Discuss about the Pitman ARE.
- 4. Write a note on merits and demerits of non-parametric tests.

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Course Code:	Course Title:	Maximum Marks : 30
PGSTAT-16(N)/MASTAT-16(N)	Econometrics	
PGSTAT-12(O)/MASTAT-12(O)		

Section- A Long Answer Questions

Note: Attempt all questions. Each question should be answered in 800 to 1000 Words.

Maximum Marks: 18

- 1. Define linear regression model with assumptions.
- 2. Discuss about the SURE model and its estimation.
- 3. What is Dummy Variable. Discuss about the use of Dummy Variables.

Section - B

Short Answer Questions

Note: Answer all questions. Answer should be given in 200 to 300 Words.

- 1. Discuss about the Point and interval Predictors.
- 2. Write shout notes on R^2 an adjusted R^2
- 3. What is multi co-linearity?
- 4. Discuss Durbin-Watson test.

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Course Code:	Course Title:	Maximum Marks : 30
PGSTAT-17(N)/MASTAT-17(N)	Demography	
PGSTAT-13(O)/MASTAT-13(O)		

Section- A Long Answer Questions

Note: Attempt all questions. Each question should be answered in 800 to 1000 Words.

Maximum Marks: 18

- 1. Discuss about the steps of construction of abridge life table Also define abridge life table.
- Define GRR and NRR. Prove that NRR≤ GRR. Give the reason why NRR is less than GRR.
- 3. Discuss about the migration. Also define estimation of internal migration from duration of residence statistics.

Section - B

Short Answer Questions

Note: Answer all questions. Answer should be given in 200 to 300 Words.

- 1. Discuss about the migration with its type and deferent methods of estimation.
- 2. Write shout notes on (a) Mean Length of Generation (b) Expectation of life
- 3. Explain basic concept of stable and stationary population.
- 4. Define IMR (Infant mortality rate) and CEB (Children ever Born).

सांख्यकी (परास्नातक) कार्यक्रम अधिन्यास सत्र 2019–20

Course Code:	Course Title: Research Methodology	Maximum Marks : 30
PGSTAT-20(N)/MASTAT-20(N)	in Social Behavior Sciences	

Section- A

Long Answer Questions

Note: Attempt all questions. Each question should be answered in 800 to 1000 Words.

Maximum Marks: 18

- 1. What is Research. Give the Criteria of a good research problem.
- 2. Discuss about the Different methods of data Collection.
- 3. Write a note on Analysis of Covariance.

Section - B

Short Answer Questions

Note: Answer all questions. Answer should be given in 200 to 300 Words.

- 1. Define (a) Critical Region (b) Level of Significance.
- 2. Write shout notes on (a) Types of Error (b) Types of Hypothesis
- 3. Write the basic principles of Experimental design.
- 4. Define Research Design.

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Course Code:	Course Title:	Maximum Marks : 30
PGSTAT-21(N)/MASTAT-21(N)	Statistical Software	

Section- A

Long Answer Questions

Note: Attempt all questions. Each question should be answered in 800 to 1000 Words.

Maximum Marks: 18

1. Volcanologist have measured the hydrogen content (in % of total number of atoms) of sample of gases collected from the 1970 and 1971 Mount Etna volcanic eruptions. Values are given in the following table:

1970 Hydrogen Content (%)		1971 Hydrogen Content(%)	
35.8	38.5	42.0	45.0
45.5	36.0	57.0	44.6
35.5	40.5	42.0	48.5
32.0	35.5	54.5	63.0
50.0	45.5	35.0	55.0
39.0	37.0	52.0	40.0
37.0	36.0	43.5	37.5
47.0	53.0	48.0	53.7

- (a) Calculate a mean hydrogen content value for the 1970 eruption and use Student's t-distribution to find the 95% confidence limits for the true value.
- (b) Use the Student's t-test for comparing means to determine whether there is a difference in the hydrogen content of the gases between the two eruption at the 99% confidence level.
- 2. If the population of shell length to width ratios of a species of bivalve is normally distributed with a mean of 1.65 and a standard deviation of 0.05, what is the probability that any one shell picked at random has a length-to-width ratio: (i) less than 1.65 (ii) within two standard deviations of the mean.
- 3. Write a MATLAB function to calculate the maximum of ten numbers.

Section - B

Short Answer Questions

Note: Answer all questions. Answer should be given in 200 to 300 Words.

Maximum Marks: 12

1. Briefly explain the use of the following commands in MATLAB:

a. grid ()

b. plot ()

c. title ()

- 2. What is an R data frame? How is it different from a matrix.
- 3. Write short notes on SPSS. Also define the Data view and variable view.
- 4. Define (i) An Ergodic Markov Chain, (ii) Stationary Markov Chain.

सांख्यकी (परारनातक) कार्यक्रम अधिन्यास सत्र 2019–20

Course Code:	Course Title - Official Statistics	Maximum Marks : 30
PGSTAT-22(N)/MASTAT-22(N)		

Section - A

Long Answer Questions

Note: Attempt any three questions. Each question should be answered in 800 to 1000 Words. Maximum Marks: 18

- 1. Discuss about the use of statistics in different fields.
- 2. Discuss about the various optical agencies responsible for data Collection.
- 3. Write an essay on the cost of living index number in India.

Section - B

Short Answer Questions

Maximum Marks: 12

Note: Attempt any four questions. Answer should be given in 200 to 300 Words.

- 1. Discuss about the principle of local control and randomization.
- 2. Discuss about the Hypothesis. Also give its types.
- 3. What is Census?
- 4. Define migration how can its effects the population of any area.